

# Public Policy Towards Network Industries

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# Focus of Analysis

- Regulation of *network infrastructure industries* such as railroads, electric power, telecommunications
  - Nature & extent of legal, regulatory constraints
- Decision criteria are economic efficiency
  - How to generate most total surplus
- This analysis requires understanding of:
  - Production costs
  - Demand characteristics
  - Informational constraints
  - Pricing Theory
  - Market Definition & market power...

# Basic Distinction

- Government interventions in markets are of two basic types:
  - *ex-ante* (regulation) *OR* *ex-post* (competition policy/anti-trust)
- Choice between these depends on:
  - Probability of need for restraint
  - Cost of punishment vs Cost of regulation
- Part I focuses on regulation, with more limited attention to anti-trust issues.
  - Unavoidable mixing because of “liberalization” of (portions of) most infrastructure networks.

# Summary and Overview: Network Characteristics and Policy Issues

- Characteristics of Network Infrastructure Industries
  - Economies of scale and scope
  - Long-lived, sunk assets
  - Vertical integration of “monopoly” and “competitive” components
  - Multiple services and/or customer classes
  - Network externalities
- Resulting Policy Problems
  - Mark-ups over cost required to break-even
  - Recovering capital investments
  - “Unbundling” (vertical disintegration) and Access pricing
  - Price discrimination and Cross-subsidization
  - Universal Service funding

# Lecture 1: Costs

Reading:

J. Panzar, “Technological Determinants of Firm and Industry Structure,” Chapter 1 in the *Handbook of Industrial Organization*

# Cost analysis forms the basis for public policy toward network industries

- *Marginal costs* are the benchmark for efficient pricing
- *Incremental costs* and *stand-alone* costs form the price floors and ceilings relevant for subsidy analysis.
- Intertemporal analysis of costs essential for understanding *total service long run incremental costs* (TSLRIC) and other regulatory “terms of art.”

# Natural monopoly and economies of scale

Natural Monopoly or  
Subadditivity of Cost:  
(at output level  $y^0$ )

$$C(y^0) \leq \sum_{i=1}^m C(y^i)$$

Economies of scale:  
(single output)

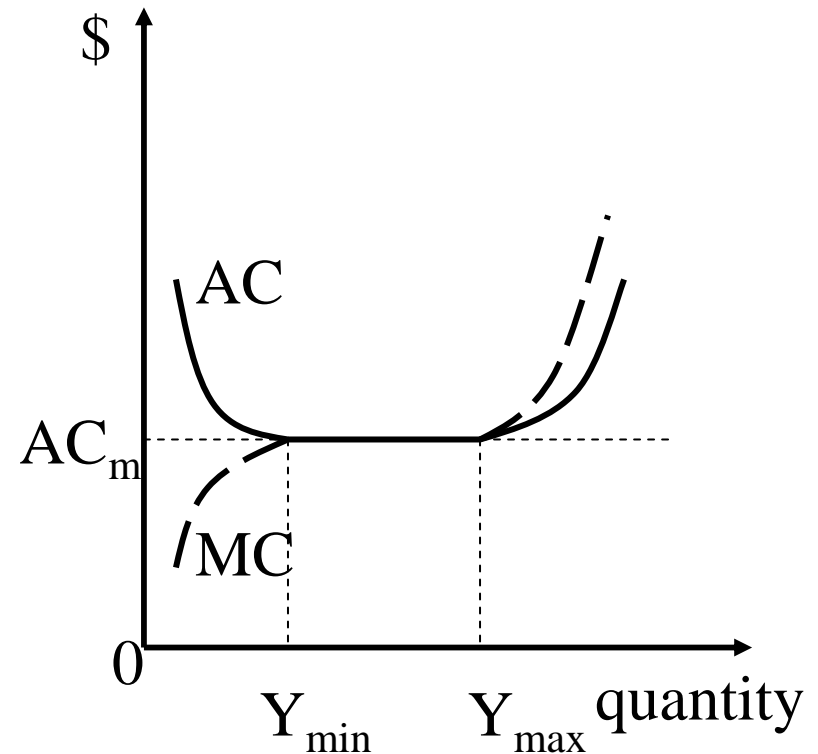
$$\sum_{i=1}^m y^i = y^0 \quad m \geq 2$$

Economies of scale  
through  $y^0$  imply NM  
at  $y^0$ , but not  
conversely

$$S(y) = \frac{AC(y)}{MC(y)} = \frac{C(y)}{yMC(y)}$$

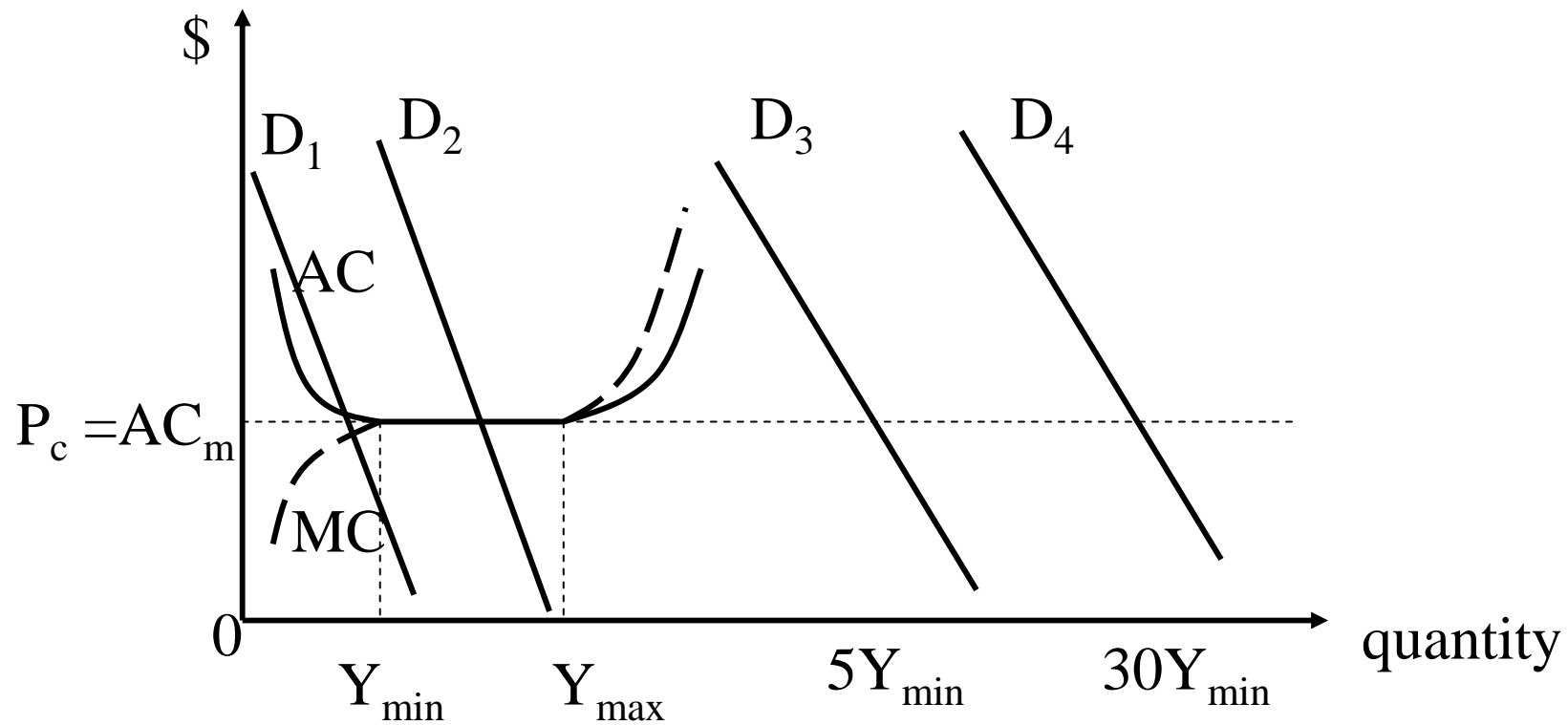
# Increasing, constant and decreasing returns to scale

- For  $Y < Y_{\min}$ ,  $AC > MC$ , unit costs are falling, and the firm enjoys *increasing returns to scale*.
- For  $Y_{\min} < Y < Y_{\max}$ ,  $AC = MC$ , unit costs are constant, and the firm experiences *constant returns to scale*.
- For  $Y > Y_{\max}$ ,  $AC < MC$ , unit costs are rising, and the firm experiences *decreasing returns to scale*.



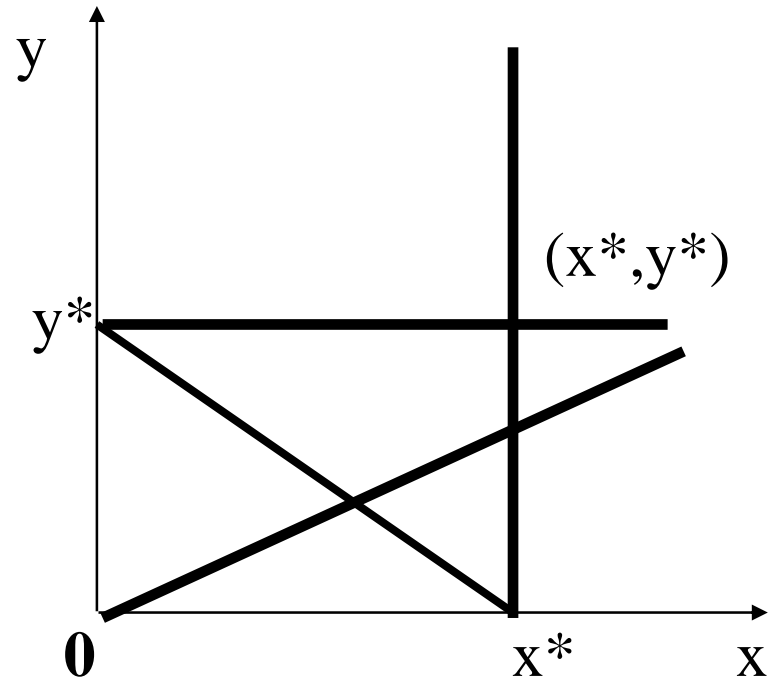


“Natural” industry structure determined by demand *relative* to min efficient scale



# Multi-product cost concepts for network industries

- Ray-average cost
- Incremental and stand-alone costs
- Product specific fixed costs
- Economies of scope
- Trans-ray convexity



# Ray-average costs and multi-product economies of scale

- RAC measure the behavior of costs along a ray through the origin.
- RAC reaches a minimum at the point of constant (multi-product) returns to scale.

$$RAC(\mathbf{y}) \equiv C(\mathbf{y}) / \mathbf{a} \cdot \mathbf{y}$$

$$\frac{dRAC(t\mathbf{y})}{dt} =$$

$$RAC(t\mathbf{y}) \left[ \frac{\sum_i y_i C_i(t\mathbf{y})}{C(t\mathbf{y})} - \frac{1}{t} \right]$$

Let  $t^*$  minimize  $RAC(t\mathbf{y})$

and normalize  $t^* = 1$ :

$$\text{Then } S(\mathbf{y}) \equiv \frac{C(\mathbf{y})}{\mathbf{y} \cdot \nabla C(\mathbf{y})} = 1$$

at minimum  $RAC$

# Multi-product economies of scale

- Marginal costs for individual products are well-defined
- Average costs for individual products are *not* well-defined
- $S$  measures the behavior of costs as all outputs vary in proportion.

$$MC_x = \frac{\partial C(x, y)}{\partial x}$$

$$MC_y = \frac{\partial C(x, y)}{\partial y}$$

$$\text{e.g. } AC_x \neq \frac{C(x, y)}{x}$$

$$S(x, y) \equiv \frac{C(x, y)}{x \cdot MC_x + y \cdot MC_y}$$

# Incremental and stand-alone costs

- Two product example: total costs =  $C(x,y)$ .
- Stand-alone costs measure the cost of producing *only* that product: e.g.,  $C(x,0)$ .
- Incremental costs are the *added* costs caused by a product: e.g.,  $IC_x = C(x,y) - C(0,y)$ .
- Average Incremental Costs *are* well-defined on a per unit basis:  $AIC_x = IC_x/x$

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- $AIC_x = IC_x/x$

Let  $S \subseteq N = \{1, \dots, n\}$

and  $\mathbf{y} \in \mathfrak{R}_+^n$ .

Define  $\mathbf{y}_S$  s.t.

$(\mathbf{y}_S)_i = y_i$  for  $i \in S$ ,

$(\mathbf{y}_S)_i = 0$  for  $i \notin S$ .

$$SAC_S(\mathbf{y}_S) = C(\mathbf{y}_S)$$

$$IC_S(\mathbf{y}) = C(\mathbf{y}) - C(\mathbf{y}_{N-S})$$

# Product specific fixed costs

- Fixed costs result from a discontinuity of the cost function at the origin.
- Product-specific fixed costs result from discontinuities along axes.

$$\text{Let } C(y) = F\{S\} + c(y)$$

*s.t.*

$$S = \{i \in N : y_i > 0\}$$

$$c \in C^2, c(\mathbf{0}) = 0$$

$$T \subseteq S \Leftrightarrow F\{T\} \leq F\{S\}$$

$$psfc_S = F\{N\} - F\{N - S\}$$

# Product specific fixed costs

- Fixed costs result from a discontinuity of the cost function at the origin.
- Product-specific fixed costs result from discontinuities along axes.
- PSFC's are part of IC

$$C(0,0) = 0$$

$$C(x, y) = F + c_x x + c_y y$$

$$C(x, 0) = F_x + c_x x$$

$$C(0, y) = F_y + c_y y$$

$$F_x, F_y \leq F \leq F_x + F_y$$

$$psfc_x = F - F_y$$

$$psfc_y = F - F_x$$



# Examples of fixed and product specific fixed costs

- Fixed costs do not vary with volume and are common to all of the firm's products:
  - General Headquarters
  - CEO's salary
- Product specific fixed costs also do not vary with volume, but can be avoid if product line shuts down
  - Divisional HQ
  - Salary of Divisional VP

# Economies of scope

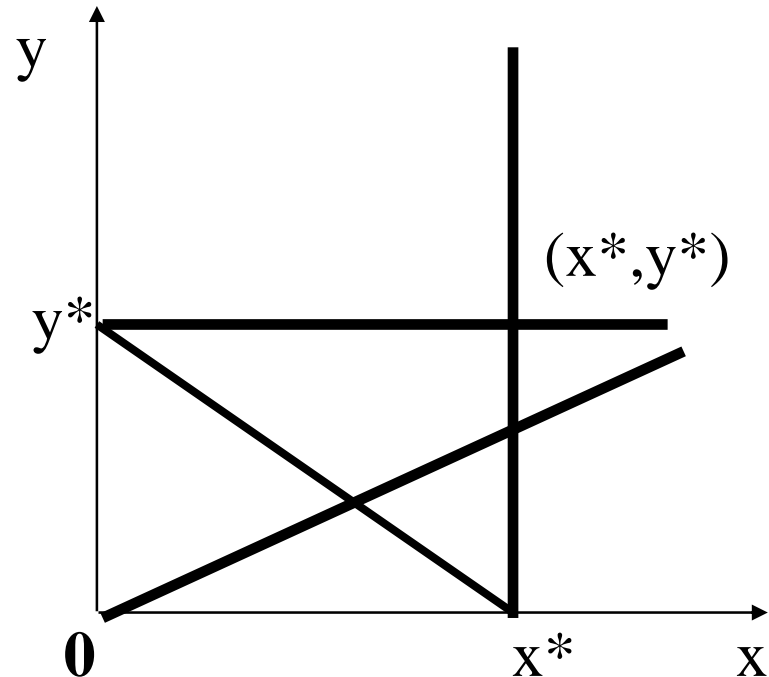
- Scope economies are present when it is cheaper to produce multiple products together:

$$C(x,0) + C(0,y) > C(x,y)$$

- Arise from shared inputs:
  - peak load structure (day/night service)
  - shared facilities
  - joint production (wool/mutton)
- Network pricing problem: apportion benefits of economies of scope among user groups

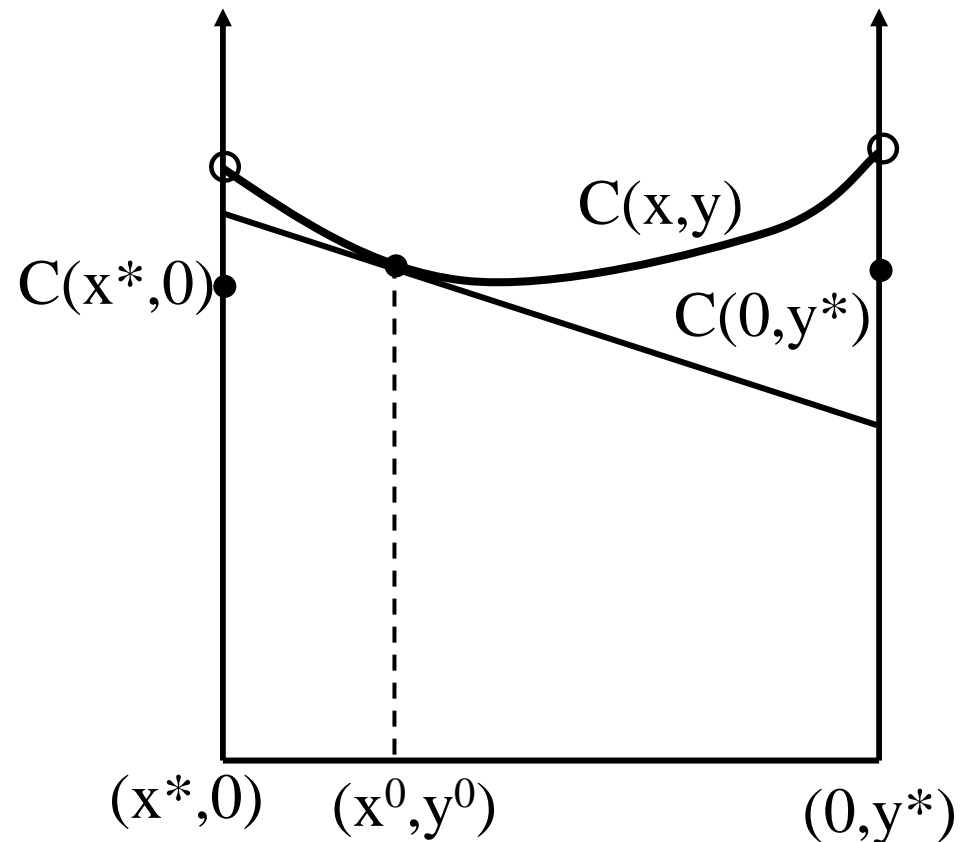
# Multi-product cost concepts for network industries

- Ray-average cost
- Incremental and stand-alone costs
- Product specific fixed costs
- Economies of scope
- Trans-ray convexity



# Trans-ray behavior

- The behavior of costs across rays reflects the extent of *complementarities*.
- Basic notion is *trans-ray supportability*
  - Does cost surface have a support at a point?
- Product specific fixed costs pose difficulties for this property
  - E.g., *without* psfc the tangent line supports the cost surface at  $(x^0, y^0)$  along the transray connecting points  $(x^*, 0)$  and  $(0, y^*)$ .

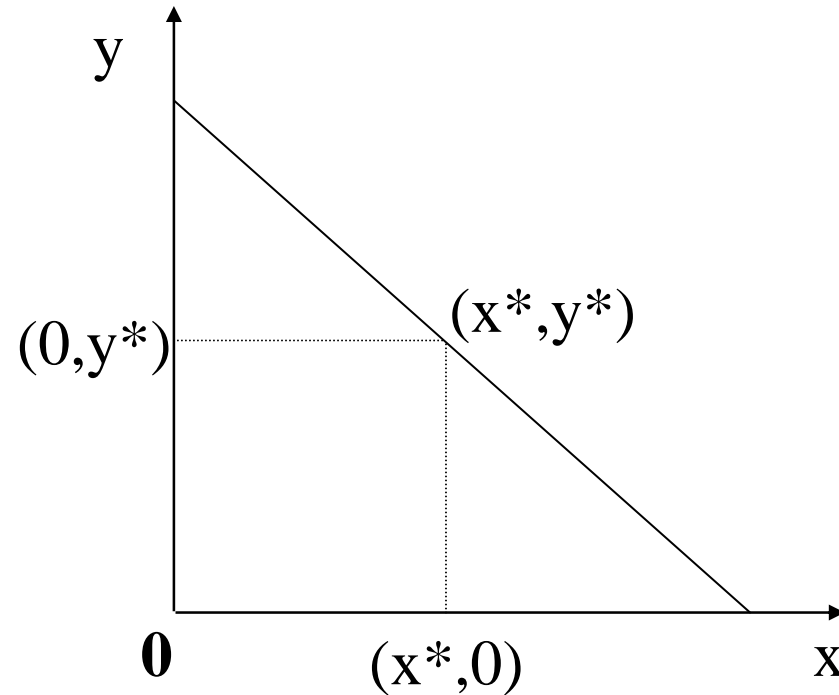


# Complementarities and submodularity

- *Weak cost complementarities* are captured by the assumption  $C_{ij}(\mathbf{y}) \leq 0$  for  $i \neq j$ .
  - Intuitively, the marginal cost of product  $i$  falls when the level of product  $j$  increases.
- A twice continuously differentiable cost function is *submodular* if it exhibits weak cost complementarities everywhere.
- More generally, a multiproduct cost function is submodular if  $C(\mathbf{y}_S + \mathbf{y}_V) - C(\mathbf{y}_S) \geq C(\mathbf{y}_T + \mathbf{y}_V) - C(\mathbf{y}_T)$  for  $S \subseteq T$
- Submodularity is *sufficient*, but *not necessary* for economies of scope to exist. (E.g., let  $S = \emptyset$ , above)

# Economies of scale, economies of scope, and natural monopoly

- Surprisingly, Ec of Scale *and* Ec of Scope do not imply Natural Monopoly.
- Two types of sufficient conditions:
  - Strengthen Ec of Scale: e.g., Declining Average Incremental Costs (DAIC)
  - Strengthen Ec of Scope: e.g., trans-ray supportability
- Exercises: 2 product proofs
  - DAIC and Ec Scope  $\Rightarrow$  NM
  - Q-Convexity of Costs and Ec of Scale  $\Rightarrow$  NM



# Implications of economies of scope and scale

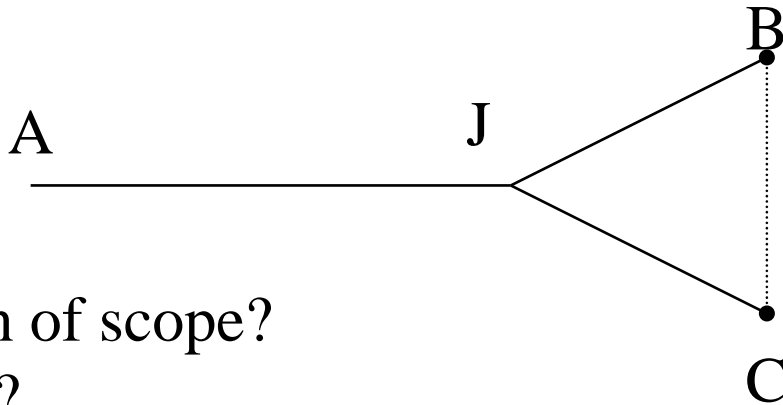
- Economies of scale mean there will be a deficit from marginal cost pricing:

$$S(x,y) > 1 \Rightarrow x \cdot MC_x + y \cdot MC_y < C(x,y)$$

- Economies of scope mean there will be a deficit from pricing at average incremental cost:

$$\begin{aligned} IC_x + IC_y &= [C(x,y) - C(0,y)] + [C(x,y) - C(x,0)] \\ &= C(x,y) - [C(x,0) + C(0,y) - C(x,y)] < C(x,y) \end{aligned}$$

# Network cost example (assume $J_B, J_C < BC < J_B + J_C$ )



Econ of scope?  
IC's?  
SAC's?

“Products:”

(1) (2) (3)  
 $Y_{AB}, Y_{AC}, Y_{BC}$

Costs (all fixed)

$AJ, JB, JC, BC$



# Examples of cost concepts in a network

- Stand alone costs:
  - $SAC_1 = AJ + JB$
  - $SAC_2 = AJ + JC$
  - $SAC_3 = BC$
- Incremental costs:
  - Individual services:  $IC_1 = IC_2 = IC_3 = 0!$
  - Subsets of services:
    - $IC_{1,2} = AJ + JB + JC - BC$  (Why not just AJ?)
    - $IC_{1,3} = JB$
    - $IC_{2,3} = JC$

# Network Economies of Scope: Several partitions to consider

- Totally separate versus joint:  
 $C\{1\}+C\{2\}+C\{3\} = (AJ+JB) + (AJ+JC) + BC > AJ+JB+JC = C\{1,2,3\}$
- All combinations of one and two:  
 $C\{1,2\}+C\{3\} = (AJ+JB+JC) + BC > AJ+JB+JC = C\{1,2,3\}$   
 $C\{1,3\}+C\{2\} = (AJ+JB+JC) + (AJ+JC) > AJ+JB+JC = C\{1,2,3\}$   
 $C\{2,3\}+C\{1\} = (AJ+JB+JC) + (AJ+JB) > AJ+JB+JC = C\{1,2,3\}$
- All partitions enjoy economies of scope in this example

# Covering costs “fairly” using *subsidy free prices*

- Basic principle: No service or group of services should pay more than their stand-alone costs.
- Example: Let  $AJ=20$ ;  $JB=JC=5$  and  $BC=6$ .
- What does the *stand-alone cost test* require?
  - $P_1 \leq 25$ ;  $P_2 \leq 25$ ; and  $P_3 \leq 6$
  - $P_1 + P_2 \leq 30$ ;  $P_1 + P_3 \leq 30$ ; and  $P_2 + P_3 \leq 30$
  - $P_1 + P_2 + P_3 = 30$  (break-even)
- Note that “equal division” ( $P_1 = P_2 = P_3 = 10$ ) won't work
- Notice the role played by the cost of link BC, even though it is not part of the efficient network.

# Economically meaningful multiproduct cost concepts

- *Total costs* of the enterprise (C) depend on all output levels
- *Marginal cost* of any service *i* ( $MC_i$ ) is the cost of producing *one more unit* of that service
- *Stand-alone costs* of a service *i* ( $SAC_i$ ) are the costs of providing *only* that service
- *Incremental costs* of any service *i* ( $IC_i$ ) are the *added* costs incurred because a service is provided
  - $IC_i = C - SAC_{\text{others}}$
- **AVERAGE COSTS** do not exist!
- Example:
  - Total and marginal costs are
$$C = F + c_1Q_1 + c_2Q_2 = 900 + 500 + 1000 = 2400$$
$$MC_1 = c_1 = 5$$
$$MC_2 = c_2 = 10$$
  - Stand-alone costs are
$$SAC_1 = F_1 + c_1Q_1 = 700 + 500 = 1200$$
$$SAC_2 = F_2 + c_2Q_2 = 500 + 1000 = 1500$$
  - Incremental costs are
$$IC_1 = C - SAC_2 = F - F_2 + c_1Q_1 = 400 + 500 = 900$$
$$IC_2 = C - SAC_1 = F - F_1 + c_2Q_2 = 200 + 1000 = 1200$$

# Fully distributed cost pricing

- FDC attempts to determine *the* costs of individual services
- Each service recovers the costs unambiguously assigned to it plus an allocated “fair share” of overhead costs
- Allocation rules base upon “objective criteria”
  - Volume
  - Attributable costs
- Example:
  - Output:  $Q_1=Q_2=100$
  - Attributable costs per unit:  $c_1=5$ ,  $c_2=10$ .
  - Overhead costs:
    - $F_1 = 700$  if *only* service 1
    - $F_2 = 500$  if *only* service 2
    - $F = 900$  if *both* provided
  - Allocation using relative volume:
$$C_1 = c_1Q_1 + Q_1F/(Q_1+Q_2) = 950$$
$$C_2 = c_2Q_2 + Q_2F/(Q_1+Q_2) = 1450$$
  - Allocation using relative attributable costs:
$$C_1 = c_1Q_1 + c_1Q_1F/(c_1Q_1+c_2Q_2) = 800$$
$$C_2 = c_2Q_2 + c_2Q_2F/(c_1Q_1+c_2Q_2) = 1600$$

# Cross-subsidization: When is a rate structure “subsidy free?”

- Total revenues equal total costs
  - If not, the *firm* is either providing or receiving a subsidy
- Revenues from a service must not exceed the *stand-alone costs* of the service
  - If they do, the service is *providing* a subsidy
- Revenues from a service must not be less than *incremental costs* of providing that service
  - If they are, the service is *receiving* a subsidy
- Total revenues equal total costs
$$p_1Q_1 + p_2Q_2 = F + c_1Q_1 + c_2Q_2 = 2400$$
$$p_1 + p_2 = 24$$
- Stand-alone cost tests
$$p_1Q_1 \leq SAC_1 = 1200$$
$$p_1 \leq 12$$
$$p_2Q_2 \leq SAC_2 = 1500$$
$$p_2 \leq 15$$
- Incremental cost tests
$$p_1Q_1 \geq IC_1 = 900$$
$$p_1 \geq 9$$
$$p_2Q_2 \geq IC_2 = 1200$$
$$p_2 \geq 12$$

# Can subsidy-free charges always be found?

- Example: 3 towns A, B, and C seeking water service
- Cost structure:
  - Any individual town can be provided at cost of  $14 = C(1)$
  - Any pair of towns can be served at a cost of  $18 = C(2)$
  - All 3 towns can be served at a cost of  $30 = C(3)$
- Economies of scope are present:
  - $18 = C(2) > 2C(1) = 28$
  - $18 + 14 = C(2) + C(1) > C(3) = 30$
- Joint service is efficient
- But, no subsidy-free charges exist that recover costs!
- Try symmetric charges of 10:
  - $10 < C(1) = 14$
  - But,  $2(10) > C(2) = 18$
- To be free of subsidy requires charges  $r_A$ ,  $r_B$ , and  $r_C$  such that
  - $r_A \leq 14$ ;  $r_B \leq 14$ ; and  $r_C \leq 14$
  - $r_A + r_B \leq 18$
  - $r_A + r_C \leq 18$
  - $r_B + r_C \leq 18$
- But, this requires  $r_A + r_B + r_C \leq 27 < 30 = C(3)$

# Policy problems posed by cross-subsidization

- What happens if subsidy-free prices are not established?
  - Incentives for inefficient entry are created
    - Entrants anticipate a profit by providing service to users *providing* a subsidy
  - Competitors of services *receiving* a subsidy complain
    - E.g., UPS and Deutsche Post
    - Claims often made, rarely proven
- Contrary to the example, subsidy-free prices can usually be found
  - But, doing so places restrictions on efficient cost recovery
- Most cross-subsidies are established politically, for non economic reasons
  - E.g., rail passenger service
  - Rural postal service